

PROBLEM SET 8, DUE DECEMBER 7TH 6TH

- (1) Prove that if  $(c, a) \in \mathbb{R}^2$  satisfies  $0 < c < 2$  and  $a^2 = c^3 - 4c + 4$ , then  $(|a|, 2 - c, c)$  occur as the three sides of a triangle.
- (2) Provide an example of a triangle with integers as sides, not similar to one of the examples in the text, having the property that the bisector in  $A$  and the median in  $B$  and the altitude in  $C$  are concurrent.